

# Which Abstractions for the Blockchain Technology?

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## Bitcoin: A Peer-to-Peer Electronic Cash System

Satoshi Nakamoto  
satoshin@gmx.com  
www.bitcoin.org

**Abstract.** A purely peer-to-peer version of electronic cash would allow online payments to be sent directly from one party to another without going through a financial institution. Digital signatures provide part of the solution, but the main benefits are lost if a trusted third party is still required to prevent double-spending. We propose a solution to the double-spending problem using a peer-to-peer network. The network timestamps transactions by hashing them into an ongoing chain of hash-based proof-of-work, forming a record that cannot be changed without redoing the proof-of-work. The longest chain not only serves as proof of the sequence of events witnessed, but proof that it came from the largest pool of CPU power. As long as a majority of CPU power is controlled by nodes that are not cooperating to attack the network, they'll generate the longest chain and outpace attackers. The network itself requires minimal structure. Messages are broadcast on a best effort basis, and nodes can leave and rejoin the network at will, accepting the longest proof-of-work chain as proof of what happened while they were gone.

# An overview of Bitcoin

- ▶ Bitcoin is a cryptocurrency and payment system
  - ▶ It allows users to anonymously exchange goods against digital currency
- ▶ All the valid transactions are recorded in a **public** ledger, the blockchain
  - ▶ Allows anyone to audit and check the integrity of all the transactions

## Ledger

```
Bob -> Alice ฿0.001  
Chunk -> Sara ฿0.05  
Eva -> Alice ฿0.009  
Alice -> John ฿0.02  
Bob -> Chunk ฿0.7  
Peter -> Bob ฿0.008  
Bob -> Alice ฿0.05  
Bob -> Alice ฿0.046  
Bob -> Alice ฿0.008
```



# Public ledgers

No trustworthy centralized control.  
Everyone

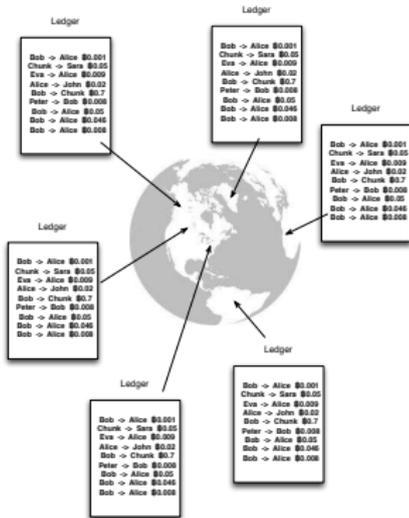
- ▶ maintains its own copy of the ledger
- ▶ disseminates all the transactions
- ▶ can read all the transactions

Achieving

- ▶ consistency and availability of the ledger

While preventing

- ▶ transaction censorship and counterfeiting (i.e., double-spending attacks)



# Content of this talk

- ▶ The addressed problem
  - ▶ Construction of a cryptocurrency and payment system with no trusted third party
- ▶ Crypto Abstractions
  - ▶ hash functions, digital signatures, hash pointers, Merkle trees
  - ▶ Application : Bitcoin transactions
- ▶ Abstractions for a distributed cryptocurrency system
  - ▶ Communication primitive
  - ▶ Application : communication in Bitcoin
  - ▶ Incentive mechanisms
  - ▶ Application : minting process in Bitcoin
  - ▶ Nakamoto Consensus
  - ▶ Application : Construction of an immutable chain of blocks
- ▶ Conclusion

# Which Abstractions?

## Digital currencies

- A string of « 0 » and « 1 »
- No central bank to prevent double spending attacks
- Solution: rely on cryptography

Crypto  
primitives



# 1. Abstraction 1 : cryptography

- ▶ cryptographic hash functions
- ▶ digital signatures
- ▶ Merkle tree

## 1.1 Hash functions

A hash function is an algorithm that allows to compute a fingerprint of fixed size from data of arbitrary size

$$\begin{aligned} H : 0, 1^* &\rightarrow 0, 1^n \\ M &\mapsto H(M) \end{aligned}$$

- ▶ rather than manipulating data of arbitrary size, a fingerprint is associated to each data which makes operation easier

## 1.1 Hash functions

A hash function satisfies the following properties

- ▶ The input space is the set of strings of arbitrarily length
  - ▶ « hello world » and « hellohellohello world » are perfectly fine inputs
- ▶ The output space is the set of strings of fixed length
  - ▶  $H(\text{« hello world »}) = 000223$
  - ▶  $H(\text{« hellohellohello world »}) = 130554$
- ▶  $H$  is deterministic
- ▶  $H$  is efficiently computable
  - ▶ Given a string  $s$  of length  $n$  the complexity to compute  $H(s)$  is  $O(n)$

In addition to these properties, crypto-hash functions have additional requirements

## 1.2 Properties of cryptographic hash functions

- ▶ Collision resistance

It must be difficult to find two inputs  $x$  and  $x'$  such that

$$H(x) = H(x')$$

- ▶ Second pre-image resistance

Given an input  $x$ , it must be difficult to find an input value

$$x' \neq x \text{ such that } H(x') = H(x)$$

- ▶ Pre-image resistance

Given  $z$ , it must be difficult to find an input value  $x$  such that

$$H(x) = z$$

# Collision resistance

collisions do exist

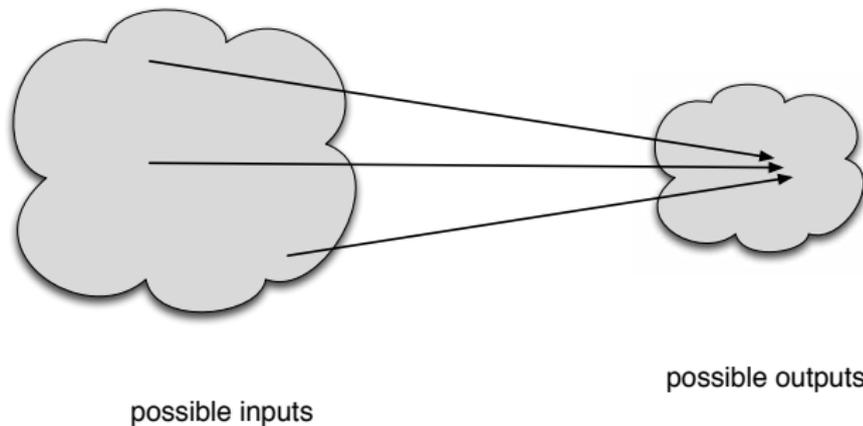


Image source: *Bitcoin and Cryptocurrency Technologies*.

but can anyone find them ?

## Collision resistance

Find two inputs  $x$  and  $x'$  such that  $H(x) = H(x')$

Generic attack (i.e., a technique capable of attacking any hash function)

- ▶ Choose  $2^{n/2}$  random messages
- ▶ Compute the hashed values and store them
- ▶ Find one pair  $(x, x')$  such that  $H(x) = H(x')$

If a computer calculates 10,000 hashes/s

- ▶ it would take  $10^{27}$  years to output  $2^{128}$  hashes, and
- ▶ thus  $10^{27}$  years to produce a collision with probability  $1/2$

Astronomical number of computations !!

So far no hash functions have been proven to be collision resistant

# Collision resistance

Collision resistant hash functions allows us

- ▶ to identify data by its hashed value (i.e digest, fingerprint)
  - ▶ if  $H(x) = H(y)$  then it is safe to assume that  $x = y$
- ▶ Bitcoin :
  - ▶ to identify transactions
  - ▶ to make blocks resistant to tampering (modifying a single bit changes the fingerprint)

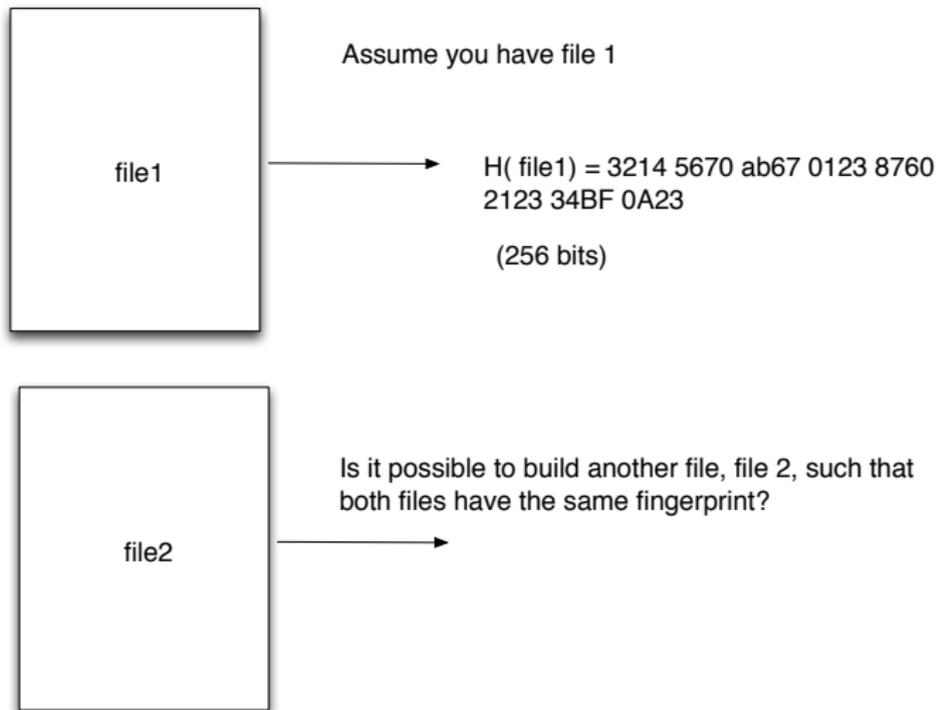
## Second-preimage resistance

Given an input  $x$ , it is difficult to find an input value  $x' \neq x$  such that  $H(x') = H(x)$

Generic Attack : probabilistic search

- ▶ Given  $x$  and its hashed value  $H(x)$  ( $n$  bits value)
- ▶ Randomly choose  $x_i$  and compute  $z_i = H(x_i)$
- ▶  $\text{Proba}(z_i = H(x)) = 1/2^n$
- ▶ Thus after having chosen  $2^n$  inputs one can find a pre-image  $x_i \neq x$  such that  $H(x_i) = H(x)$

# File integrity



## Preimage resistance

Given  $z$ , find an input value  $x$  such that  $H(x) = z$

Generic Attack : probabilistic search

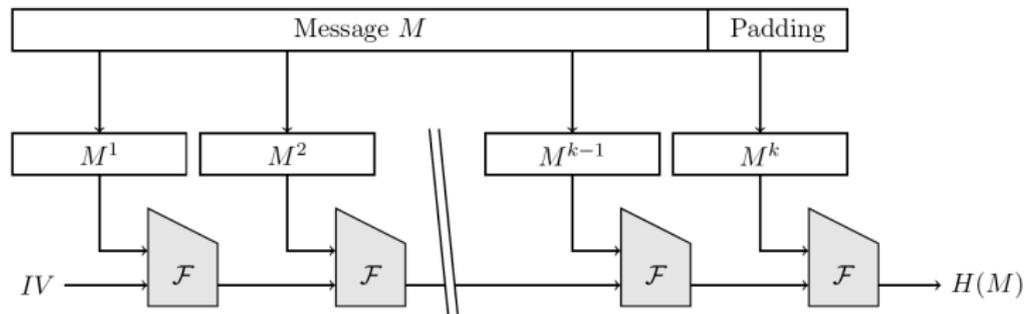
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- ▶ Randomly choose  $x_i$  and compute  $z_i = H(x_i)$
- ▶  $\text{Proba}(z_i = z) = 1/2^n$
- ▶ Thus after having chosen  $2^n$  inputs one can find a pre-image  $x_i$  such that  $H(x_i) = z$

## Password storage

- ▶ In your machine, passwords are not stored. Only their hashed values are stored
- ▶ When you want to authenticate, the login pg computes the hashed value, which is compared with the one stored in `/etc/passwd`

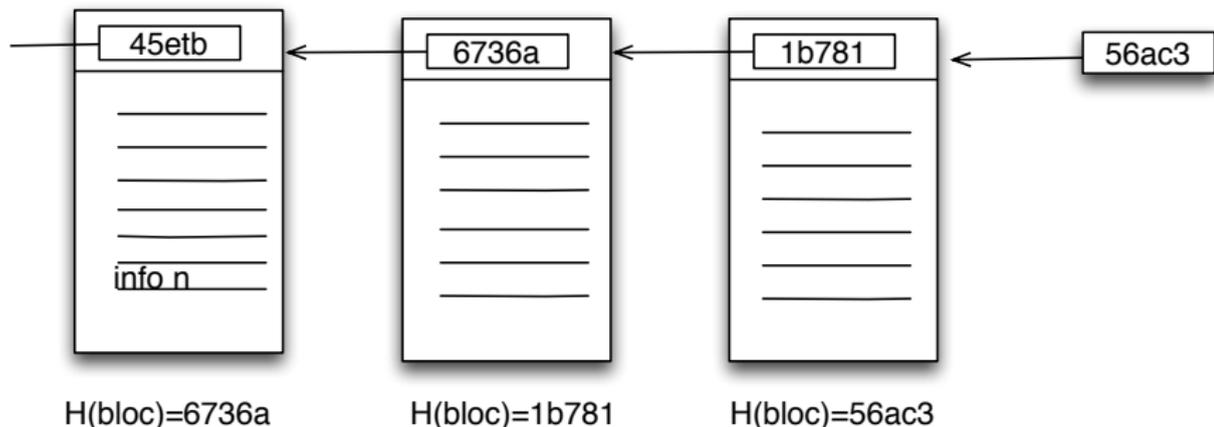
Property : Given the hashed value  $y$  it must be difficult to find  $x$  such that  $H(x) = H(\text{password}) = y$

# Merkle-Damgard construction



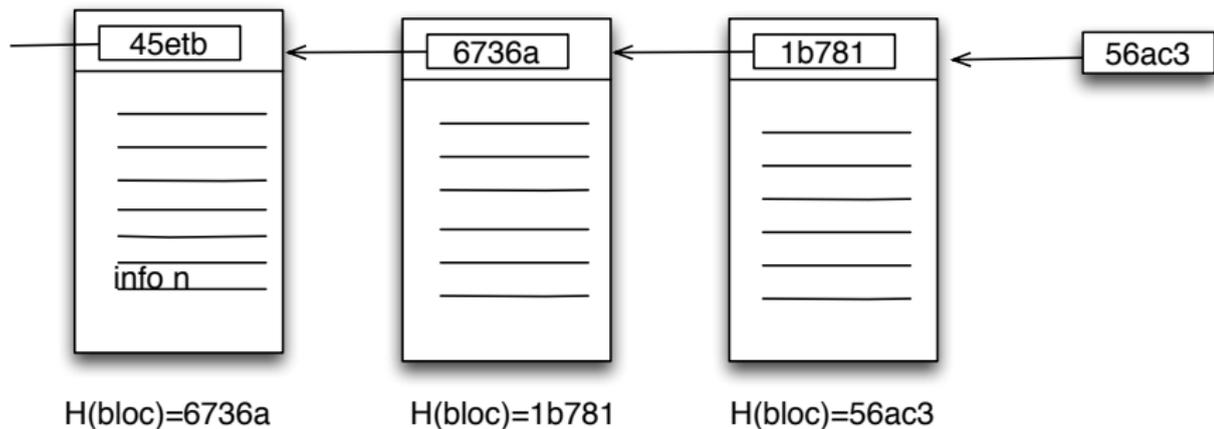
## 1.2 Hash pointers

A hash pointer is the cryptographic hash value of the pointed information



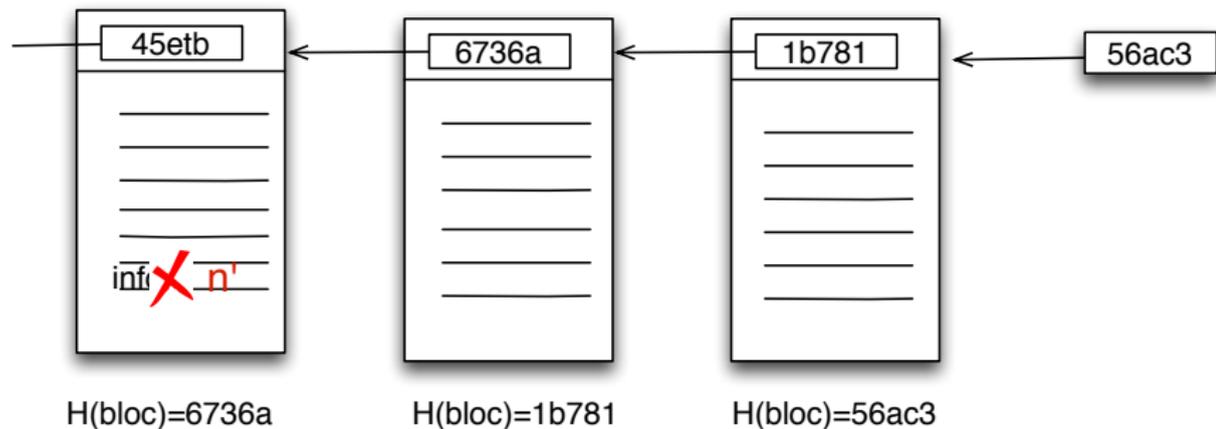
## 1.2 Hash pointers

Hash pointers allows the construction of a log data structure that allows the detection of any manipulation



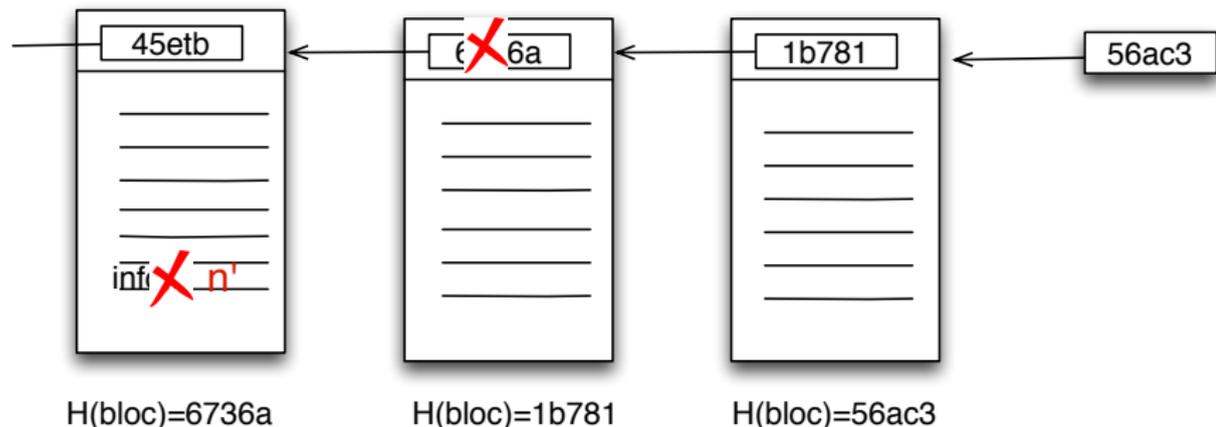
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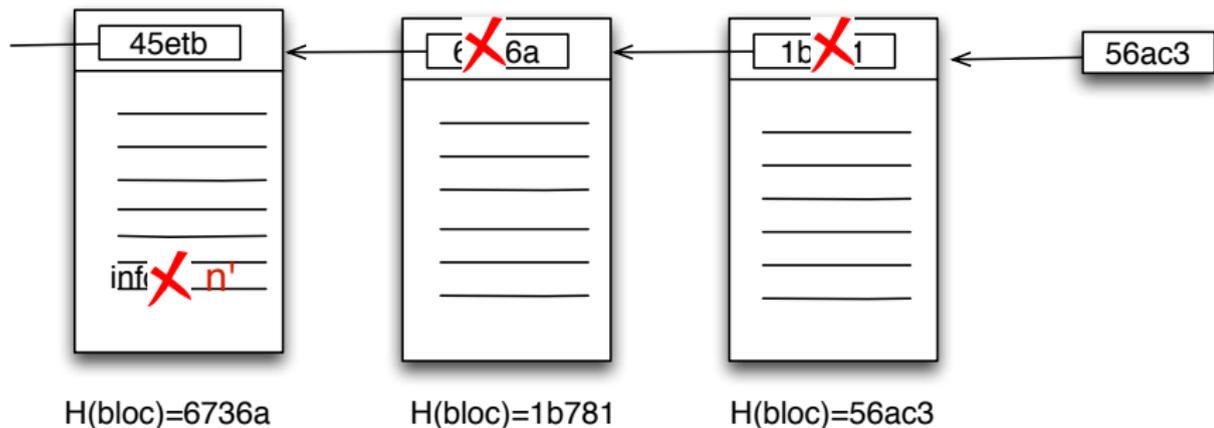
## 1.2 Hash pointers

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Hash pointers allows the construction of a log data structure that allows the detection of any manipulations



- ✓ By only keeping the hash pointer of the head of the data structure, we have a tamper-evident hash of a possibly very long list

## 1.3 Hash tree : Merkle Tree

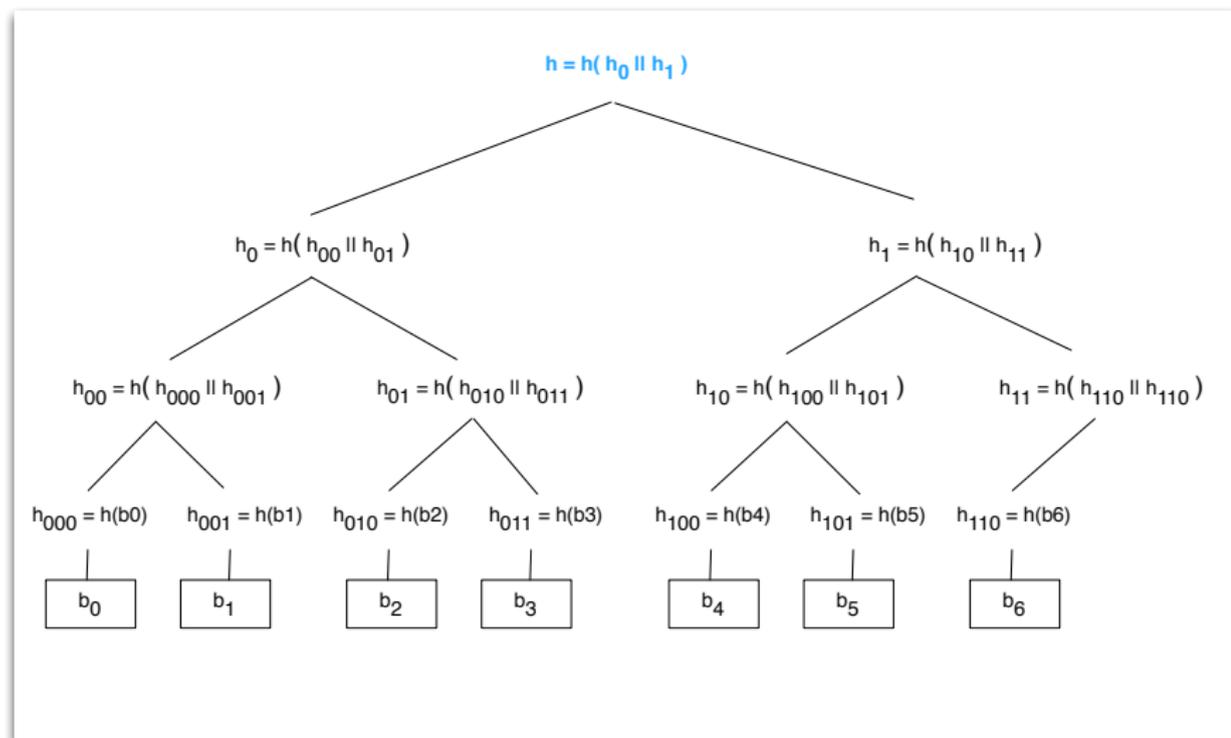
A **Merkle tree**<sup>1</sup> is a tree of hashes

- ▶ Leaves of the tree are data blocks
- ▶ Nodes are the hashes of their children
- ▶ Root of tree is the fingerprint of the tree

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1. Merkle, R. C. (1988). "A Digital Signature Based on a Conventional Encryption Function". Advances in Cryptology - CRYPTO '87.

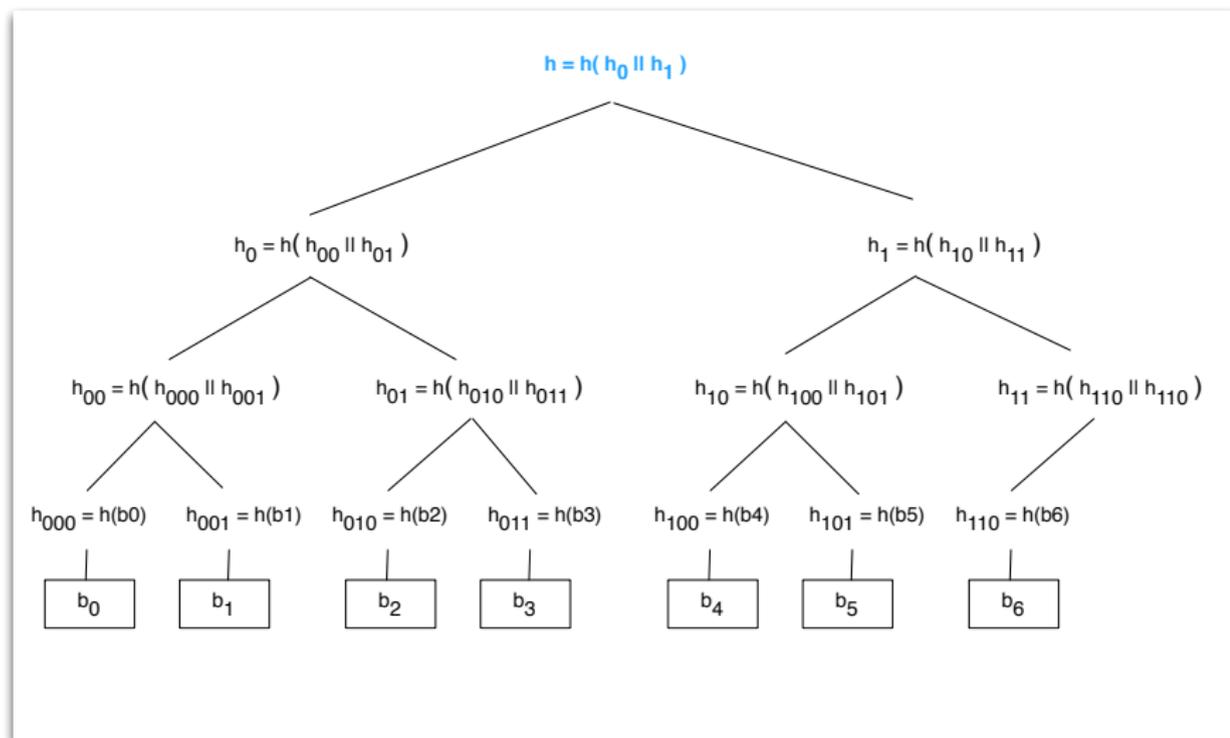
## 1.3 Hash tree : Merkle Tree



## 1.3 Hash tree : Merkle Tree

- ✓ Checking the integrity of the  $n$  data blocks of the tree
  - ▶ easy due to collision resistance property of crypto. hash functions
- ✓ Data blocks membership
  - ▶ checked with  $\log n$  pieces of information and in  $\log n$  operations

## 1.3 Hash tree : Merkle Tree



## 1.4 Digital signature primitive

A digital signature is just like a signature on a document

- ▶ Only the creator of the document can sign, but anyone can verify it
- ▶ Signature is tied to a particular document

How can we build such a digital signature?

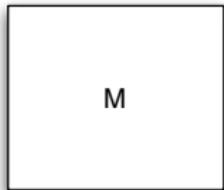
## 1.4 Digital signature

Three functions :

- ▶  $(s_k, p_k) := \text{generateKeys}(\text{keysize})$ 
  - ▶  $s_k$  : **private** signing key
  - ▶  $p_k$  : **public** verification key
- ▶  $\text{sig} := \text{sign}(s_k, H(\text{message}))$
- ▶  $\text{ver} := \text{verify}(p_k, \text{sig})$

# 1.4 Digital signature

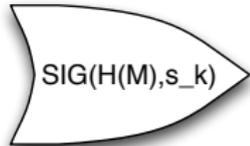
Alice



$H(M)$



$H(M) = 01011011$



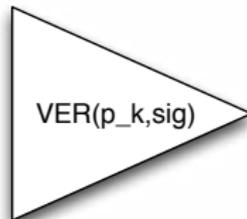
$= sig$

$(M, sig)$



$H(M)$

Bob



$= ver$

if  $(ver = H(M))$  then sig is valid

# Using verification public key as an identity

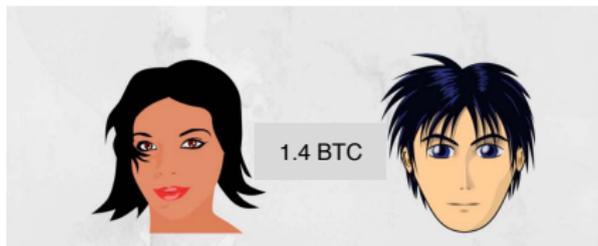
Idea<sup>2</sup>

- ▶ If you see  $(m, sig)$  such that the signature verifies under  $p_k$  (i.e.  $verify(p_k, sig) = true$ ) then one can see  $p_k$  as a party saying statements by signing them

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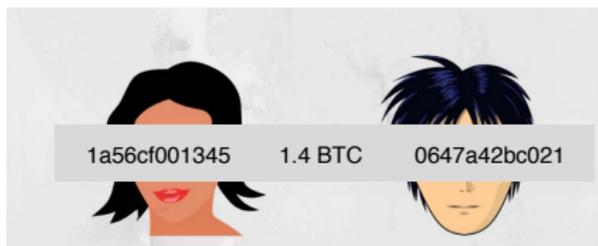
2. D. Chaum, « Untraceable Electronic Mail, Return Addresses, and Digital Pseudonyms », Communications of the ACM 24(2), pp :84–90,1981

## No identities



- ▶ Alice and Bob want to transfer values
- ▶ But Alice does not want to use neither her identity nor Bob's one in the transaction

## Using verification public key as identities



- ▶ If you see a msg such that the signature verifies under  $p_k$  (i.e.  $verify(p_k, msg, sig) = true$ ) then one can see  $p_k$  as a party saying statements by signing them
- ▶ To speak on behalf of  $p_k$  one must know  $s_k$
- ▶ So there is an identity in the system such that only a single one can speak for it<sup>3</sup>

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3. D. Chaum, « Untraceable Electronic Mail, Return Addresses, and Digital Pseudonyms », Communications of the ACM 24(2), pp :84–90,1981

## Using Verification public key as identities



- ✓ By looking at public keys as identities you can generate as many identities as you want !
- ✓ No central authority in charge of registering them !

## Using verification public key as an identity

What about privacy?

- ▶ no relationships between  $p_k$  based identities and real identities
- ▶ by using the same  $p_k$  (identity) an adversary can infer some relationships based on the activity of  $p_k$

## Using the « public key as identity » principle in crypto-payment systems

- ▶ Most of the crypto-currencies use this principle to handle accounts
- ▶ An account is a pair  $(p_k, s_k)$  and an amount of coins

# First detour to Bitcoin : Transactions

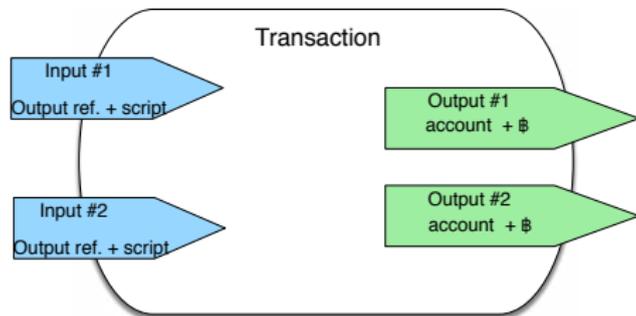
- ▶ Transactions : state of the crypto-currency system
  - ▶ data structure that allows Alice to transfer bitcoins to Bob and Charly
  - ▶ does not contain any confidential information
  - ▶ verifiable by anyone → no trusted third-party!

## Transaction : account

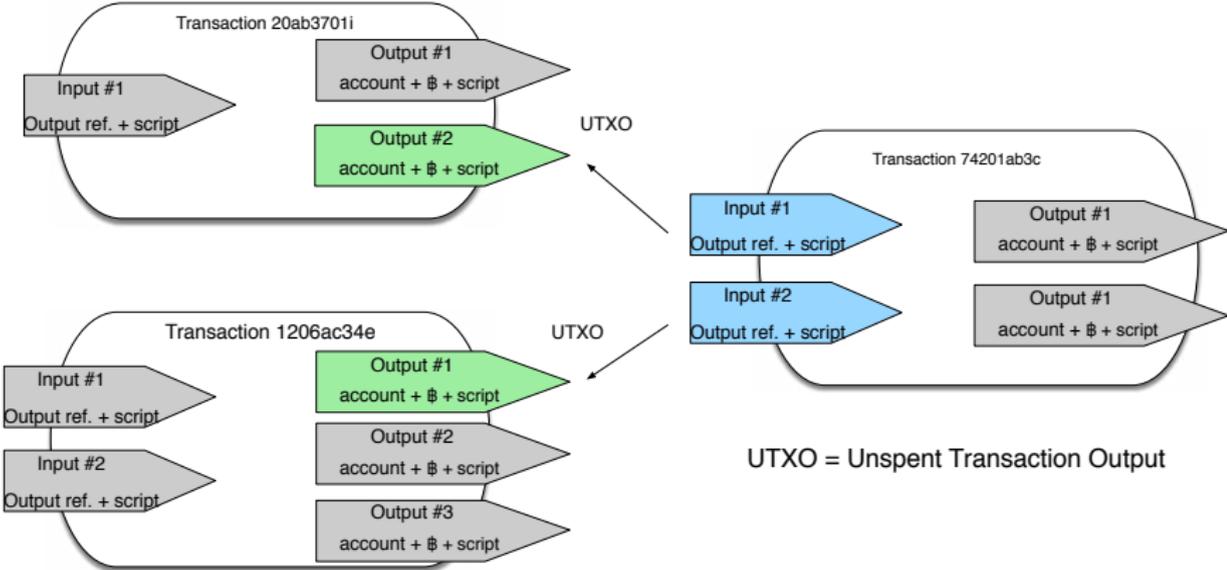
- ▶ An account is a « one shot object »
  - ▶ an account is a <(private key,public key), amount of bitcoins>
  - ▶ relies on the *public key as identity* principle
  - ▶ debited once!
  - ▶ each time you are the recipient of a transaction, it's safer if you create a new account (privacy reasons)

# Transaction : structure

- ▶ Alice's account  
(input address)
- ▶ Bob's and Charly's  
accounts (output  
address)
- ▶ possibly some  
change
- ▶ transactions fees



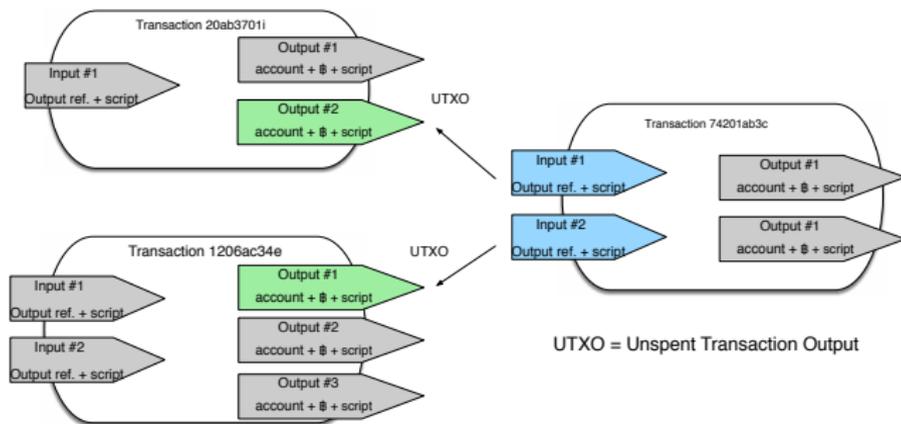
# Relying on past transactions to create new ones



Do not forget Tx fees, i.e., ₿ input > ₿ output

# Transaction : script

- ▶ Bitcoin relies on a (limited) script language
- ▶ to lock an output, the script provides a challenge
  - ▶ *i.e.*, fingerprint of the recipient public key,  $H(p_k)$
- ▶ to unlock an input, the script provides the solution of the challenge
  - ▶ *i.e.*, public key  $p_k$  together with  $s_k$ 's signature



Do not forget Tx fees, *i.e.*, ₿ input > ₿ output

# Script language

Decoded:

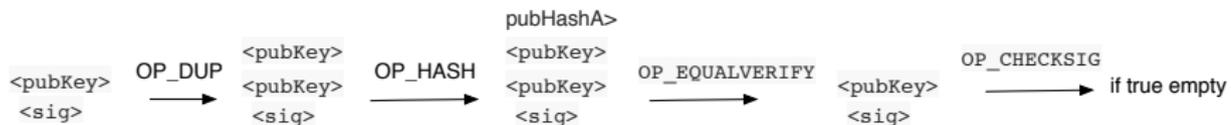
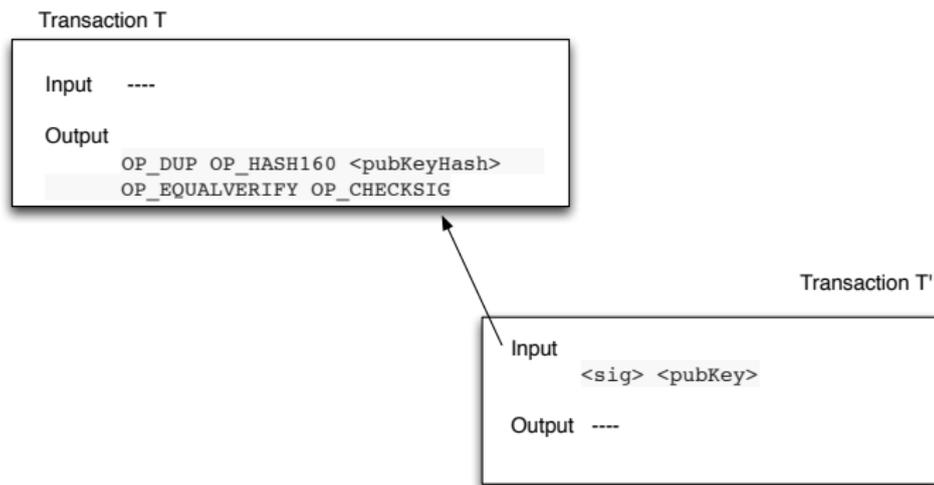
- Header: ver=1, vin.size=1, vout.size=2, nLockTime=438069
- Inputs:
  - ID: 4983442ccd814372b8c8614bf81942ba17c6e3470f21897524a63caf54aa54ba
  - Index: 1 (input value: 0.030 980 35 BTC)
  - scriptSig:
    - Signature: 304402201e0b0555330b9ba6dc689aeebecf0464391a882c41a6650ab66f803179860a1802207d1b46c45d37e8a88fee49c3e02adb9cd3ccb4bb96ca313135e00a5c01f71a6b[ALL]
    - Key: 02374f390070a14763707fe9310a73eaf2b2221734d0ff0a0684078571e2a12e9e
  - nSeq: 4294967294

# Script language

Decoded (ctd):

- Outputs:
  - n: 0
    - value: 0.01685815 BTC
    - ScriptPubKey: OP\_DUP OP\_HASH160 3d5b9da23ff21a211f101ee2adec37d6b797db7c OP\_EQUALVERIFY OP\_CHECKSIG
  - n: 1
    - value: 0.01000000 BTC
    - ScriptPubKey: OP\_DUP OP\_HASH160 4ce03f31d4bdbbc2932f14cea99f4d96edcdebef0c OP\_EQUALVERIFY OP\_CHECKSIG

# Script language



# Which Abstractions?

Crypto  
primitives

Hash function  
Digital signature  
Merkle tree

Broadcast  
primitive

Dissemination of  
information in the  
open Bitcoin network

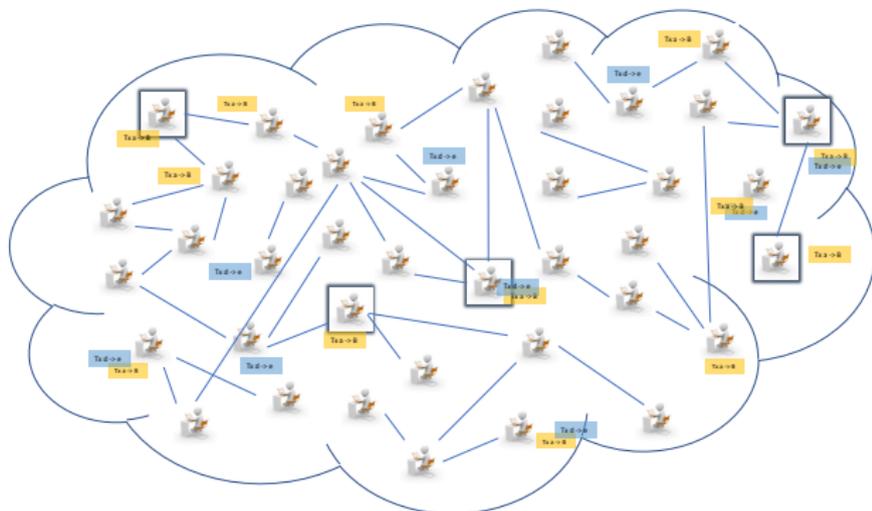


## Abstraction 2 : Communication primitive

- ▶ Size : set of thousands or millions of nodes  $\mathcal{N}$
- ▶ Dynamic : nodes can join and leave the system at will
- ▶ Randomness is fundamental
- ▶ Any individual in the system should have the same probability to be chosen as a neighbor of any other individual

# Bitcoin Network

- ▶ Peer-to-peer network<sup>d</sup>
- ▶ Topology formed through a randomized process
- ▶ No coordinating entity
- ▶ Broadcast is based on flooding/gossiping neighbors' link



## Abstraction 2 : properties

1. Fully decentralized
2. Uniformity
3. Low latency<sup>4</sup>

$$\frac{\text{msg. transmission time}}{\text{block time interval}} \ll 1$$

- ✓ Allows to keep the probability of fork small (i.e.  $10^{-3}$ )
- ✓ PoW mechanism allows this ratio to continuously hold

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4. J. Garay and A. Kiayias, The Bitcoin Backbone Protocol : Analysis and Application, Eurocrypt 2015

# Which Abstractions ?

Crypto  
primitives

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Digital signature  
Merkle tree

Broadcast  
primitive

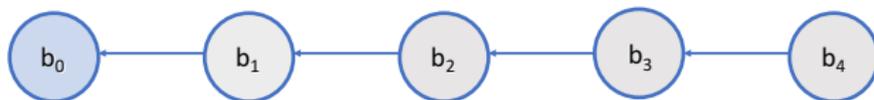
Dissemination of  
information in the  
open Bitcoin network

Agreement

Persistent ordering of  
all the transactions  
ever created with no  
trusted party

## Abstraction 3 : Agreement on the content of the ledger

A publicly, immutable, and ordered log of transactions



# Block of transactions



Transaction 945846  
Transaction 58801a  
Transaction 665389  
Transaction 7654ab  
.  
.  
.  
Transaction 321456

# Blocks of transactions

Transaction 945846  
Transaction 58801a  
Transaction 665389  
Transaction 7654ab  
.  
.  
.  
Transaction 321456

Transaction 437621  
Transaction 8593ab  
Transaction 12367b  
Transaction 793154  
.  
.  
.  
Transaction 653278

Transaction 336789  
Transaction 7245ab  
Transaction 635566  
Transaction 12f4a22  
.  
.  
.  
Transaction 232356

# Resistant to attacks



Transaction 437621  
Transaction 8593ab  
Transaction 12367b  
Transaction 793154  
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Transaction 653278

Transaction 336789  
Transaction 7245ab  
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Transaction 232356



# Resistant to attacks

T  
T  
T Transaction 945846  
T Transaction 58801a  
Transaction 665389  
Transaction **7654ab**  
T  
Transaction 321456

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# A chain of blocks : the blockchain

A publicly, immutable, and totally ordered log of transactions

- ▶ Why digital signatures are not sufficient ?
- ▶ How can we securely link blocks ?
- ▶ How can we prevent transactions in a block from being manipulated ?
- ▶ Who is allowed to create blocks ?
- ▶ Who is in charge of checking that blocks are correctly created ?

# A chain of blocks : the blockchain

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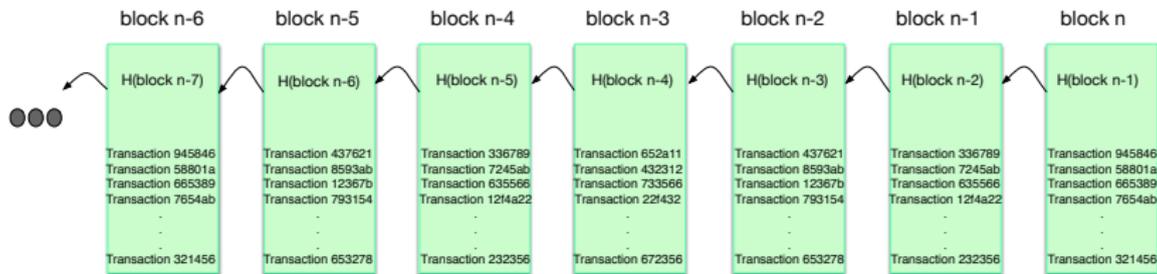
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  - ✓ efficient cryptographic fingerprint of the transactions
- ▶ Who is allowed to create blocks ?
  - ✓ any node in the network capable of solving a given challenge
- ▶ Who is in charge of checking that blocks are correctly created ?
  - ✓ everyone !!

# How can we securely link blocks ?

## Cryptographic Hash functions

- ▶ allows you to compute a fixed-size fingerprint from any type of data
- ▶ deterministic function
- ▶ efficiently computable
- ▶ practically impossible to invert (« one-way function »)

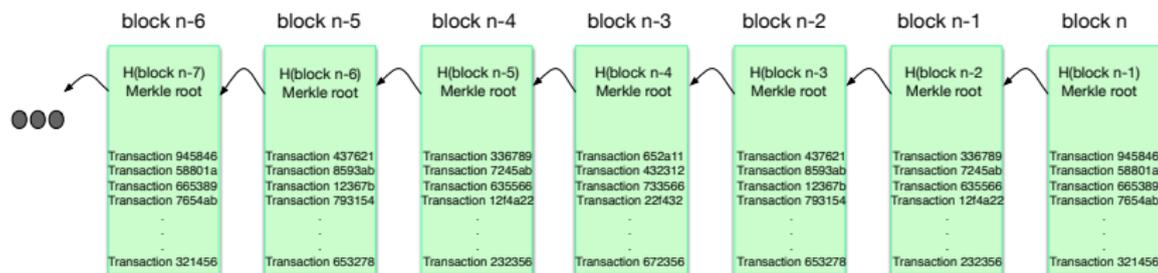


# How can we prevent transactions of a block from being manipulated?

## Merkle tree

A Merkle tree<sup>5</sup> is a tree

- ▶ Leaves of the tree are data blocks
- ▶ Nodes are the cryptographic hashes of their children
- ▶ Root of tree is the fingerprint of the tree



# Nakamoto Consensus protocol : Adversary model<sup>6</sup>

The **Computational Threshold Adversary (CTA)** model

- ▶ The adversary controls a minority of the total amount of computational power
- ▶ The CTA model is also called the permissionless model
  - ▶ There is no membership protocol
  - ▶ Incorporates some degree of synchrony

The **Stake Threshold Adversary (STA)** model

- ▶ The adversary controls a minority stake in some limited resource, i.e., the crypto-currency
- ▶ May allow to punish malicious parties via some stake deposit

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6. Ittai Abraham and Dahlia Malkhi, « The blockchain consensus layer and BFT », The distributed Computing Column, 2017

# Nakamoto Consensus protocol

The goal of the Consensus Nakamoto protocol is to implement a blockchain replication protocol<sup>7</sup>

- ▶ (Uniqueness) There is a unique chain of blocks (i.e., the blockchain)
- ▶ (Liveness) The blockchain is constantly growing
- ▶ (Safety) The deeper a block is buried in the blockchain the harder it is to abort it
- ▶ (Fairness) The proportion of blocks of non-faulty parties in the blockchain is proportional to their computation power

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7. J. Garay and A. Kiayias, The Bitcoin Backbone Protocol : Analysis and Application, Eurocrypt 2015

# Nakamoto Consensus protocol

Two ingredients : Leader Election Oracle + Heavier Fork Strategy

- 1 A leader election oracle implemented by the PoW mechanism
  - ▶ Each party is elected independently
  - ▶ The probability of electing each party is proportional to its relative computational power

→ Synchronize the creation of blocks

→ Prevent Sybil attacks

→ Incentivize correct behavior through currency creation

# Nakamoto Consensus protocol

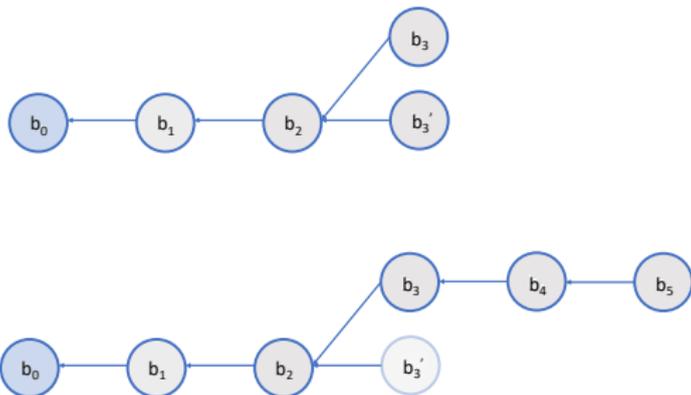
Two ingredients : Leader Election Oracle + Heavier Fork Strategy

## 2 The simple and local Heavier Fork Strategy

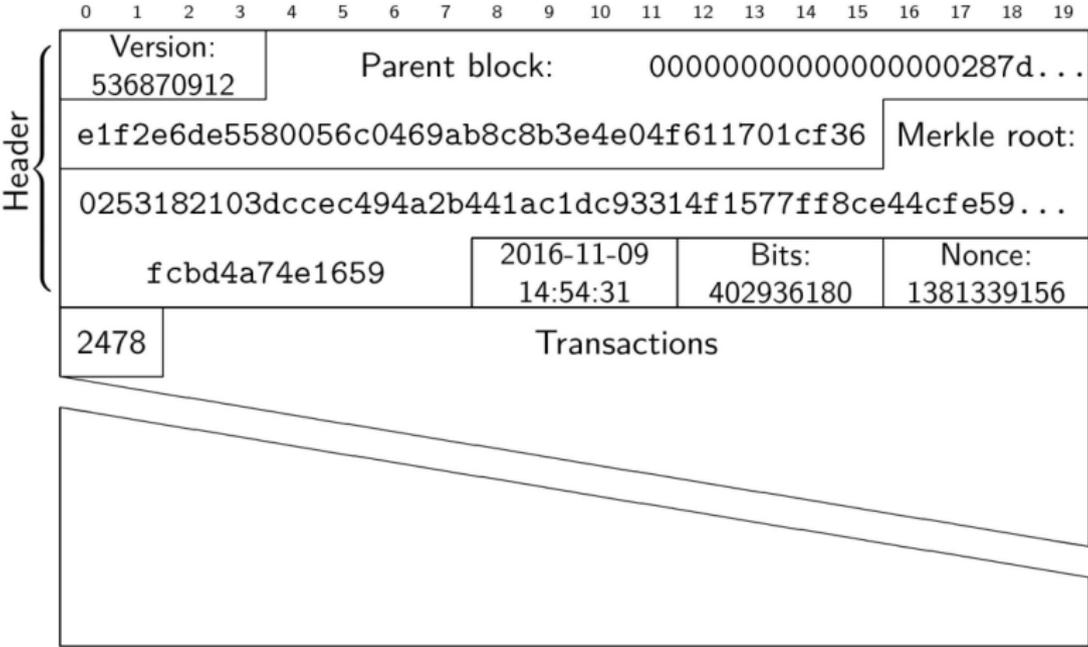
- ▶ Select the chain which required the greatest amount of work
- ▶ Random nature of the PoW + Non-faulty leaders always use the chain which required the greatest amount of work

→ One chain will be extended more than the others

→ This is the blockchain !



# Blockchain Proof-of-Work



# Blockchain Proof-of-Work

0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19
Version: 536870912				Parent block: 00000000000000000287d...															
e1f2e6de5580056c0469ab8c8b3e4e04f611701cf36														Merkle root:					
0253182103dccec494a2b441ac1dc93314f1577ff8ce44cfe59...																			
fcbd4a74e1659								2016-11-09 14:54:31				Bits: 402936180				Nonce			

Goal:  $\text{SHA256} \circ \text{SHA256}(\text{header}) \leq \text{target}$

Every 2016 blocks:

$$\text{target} \leftarrow \text{target} * \max\left(\frac{1}{4}, \min\left(4, \frac{\text{real}}{\text{expected}}\right)\right)$$

- ▶ Comes down to compute a hash partial inversion
  - ▶ find pre-image for a partially specified hash function output

0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19
Version: 536870912				Parent block: 0000000000000000000000000287d...															
e1f2e6de5580056c0469ab8c8b3e4e04f611701cf36														Merkle root: 0253182103dccec494a2b441ac1dc93314f1577ff8ce44cfe59...					
fcbd4a74e1659								2016-11-09 14:54:31				Bits: 402936180				Nonce			

Goal:  $\text{SHA}_{256} \circ \text{SHA}_{256}(\text{header}) \leq \text{target}$

Every 2016 blocks:

$$\text{target} \leftarrow \text{target} * \max\left(\frac{1}{4}, \min\left(4, \frac{\text{real}}{\text{expected}}\right)\right)$$

Each party tries to provide a pow, and the proba  $p$  that one try is successful is

$$p = D/2^\kappa,$$

with  $\{0, 1\}^\kappa$  the range of  $H(\cdot)$ , and  $D$  the difficulty.

# Proof-of-Work

string=HelloWorld!, nonce=0, difficulty=000

# Proof-of-Work

string=HelloWorld!, nonce=0, difficulty=000



HelloWorld!0:3f6fc92516327a1cc4d3dca5ab2b27aeedf2d459a77fa06fd3c6b19fb6

# Proof-of-Work

string=HelloWorld!, nonce=1, difficulty=000



HelloWorld!**0**:3f6fc92516327a1cc4d3dca5ab2b27aedef2d459a77fa06fd3c6b19fb6

HelloWorld!**1**:b5690c48c2d0a09481186aaa99e4e090901ff2ac4d572e6706dfd30eef

# Proof-of-Work

string=HelloWorld!, nonce=2, difficulty=000



HelloWorld!**0**:3f6fc92516327a1cc4d3dca5ab2b27aeedf2d459a77fa06fd3c6b19fb6

HelloWorld!**1**:b5690c48c2d0a09481186aaa99e4e090901ff2ac4d572e6706dfd30eef

HelloWorld!**2**:5b6fd9c27fcb54ca23404d9428f081b7c9280ba6370e33a6a20b16f40c

# Proof-of-Work

string=HelloWorld!, nonce=3, difficulty=000



HelloWorld!**0**:3f6fc92516327a1cc4d3dca5ab2b27aeedf2d459a77fa06fd3c6b19fb6

HelloWorld!**1**:b5690c48c2d0a09481186aaa99e4e090901ff2ac4d572e6706dfd30eef

HelloWorld!**2**:5b6fd9c27fcb54ca23404d9428f081b7c9280ba6370e33a6a20b16f40c

HelloWorld!**3**:9c5d769416aa0ca894abf22bd17bd30fbb6959291423ae1903a9f86a1f

....

# Proof-of-Work

string=HelloWorld!, nonce=94, difficulty=000



```
HelloWorld!0:3f6fc92516327a1cc4d3dca5ab2b27aeedf2d459a77fa06fd3c6b19fb6
HelloWorld!1:b5690c48c2d0a09481186aaa99e4e090901ff2ac4d572e6706dfd30eef
HelloWorld!2:5b6fd9c27fcb54ca23404d9428f081b7c9280ba6370e33a6a20b16f40c
HelloWorld!3:9c5d769416aa0ca894abf22bd17bd30fbb6959291423ae1903a9f86a1f
...
HelloWorld!94:7090a0e5d88cff635e42ea33fcd6091a058e9cdd58ab8cd5c21c1c704
```

# Proof-of-Work

string=HelloWorld!, nonce=95, difficulty=000



```
HelloWorld!0:3f6fc92516327a1cc4d3dca5ab2b27aeedf2d459a77fa06fd3c6b19fb6
HelloWorld!1:b5690c48c2d0a09481186aaa99e4e090901ff2ac4d572e6706dfd30eef
HelloWorld!2:5b6fd9c27fcb54ca23404d9428f081b7c9280ba6370e33a6a20b16f40c
HelloWorld!3:9c5d769416aa0ca894abf22bd17bd30fbb6959291423ae1903a9f86a1f
. . . .
HelloWorld!94:7090a0e5d88cff635e42ea33fcd6091a058e9cdd58ab8cd5c21c1c704
HelloWorld!95:b74f3b2cf1061895f880a99d1d0249a8cedf223d3ed061150548aa621
HelloWorld!96:447ca2fa886965af084808d22116edde4383cbaa16fd1fbcf3db61421
```

# Proof-of-Work

string=HelloWorld!, nonce=97, difficulty=000,



HelloWorld!**0**:3f6fc92516327a1cc4d3dca5ab2b27aeedf2d459a77fa06fd3c6b19fb6

HelloWorld!**1**:b5690c48c2d0a09481186aaa99e4e090901ff2ac4d572e6706dfd30eef

HelloWorld!**2**:5b6fd9c27fcb54ca23404d9428f081b7c9280ba6370e33a6a20b16f40c

HelloWorld!**3**:9c5d769416aa0ca894abf22bd17bd30fbb6959291423ae1903a9f86a1f

....

HelloWorld!**94**:7090a0e5d88cff635e42ea33fcd6091a058e9cdd58ab8cd5c21c1c704

HelloWorld!**95**:b74f3b2cf1061895f880a99d1d0249a8cedf223d3ed061150548aa621

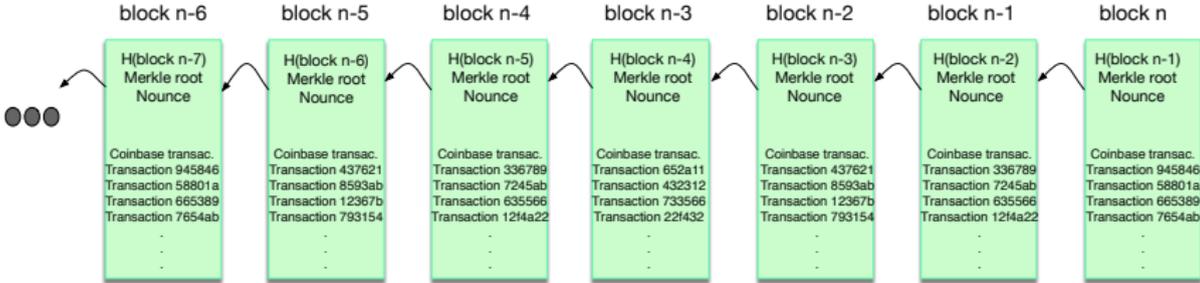
HelloWorld!**96**:447ca2fa886965af084808d22116edde4383cbaa16fd1fbcf3db61421

HelloWorld!**97**:**000**ba61ca46d1d317684925a0ef070e30193ff5fa6124aff76f513d96

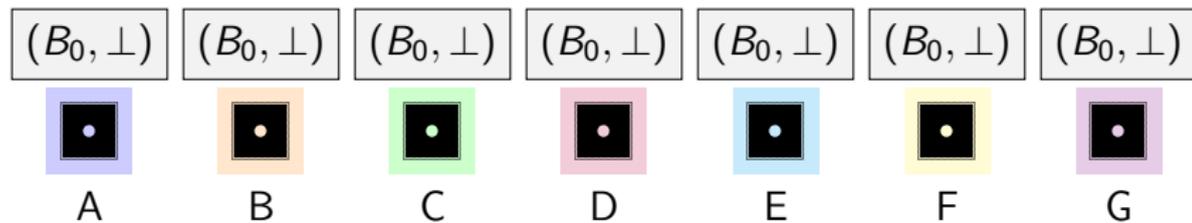
# Blockchain Proof-of-Work

## Properties

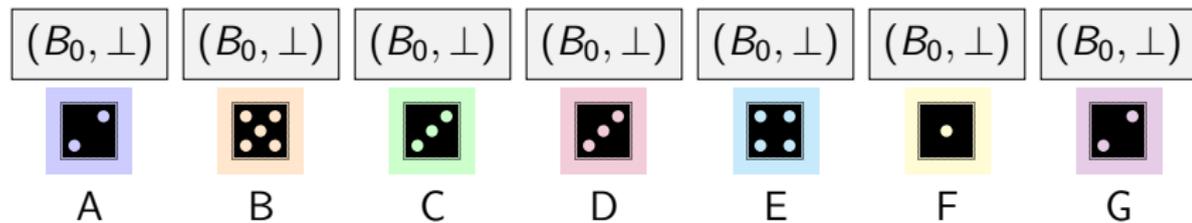
- ▶ Algorithmically computable
- ▶ Difficult to solve but quickly verified
- ▶ Difficulty proportional to computation power
  - ▶ average generation time : 10 minutes
  - ▶ proba that one try is successful is proportional to the difficulty and the range of  $H(.)$
- ▶ Memoryless process



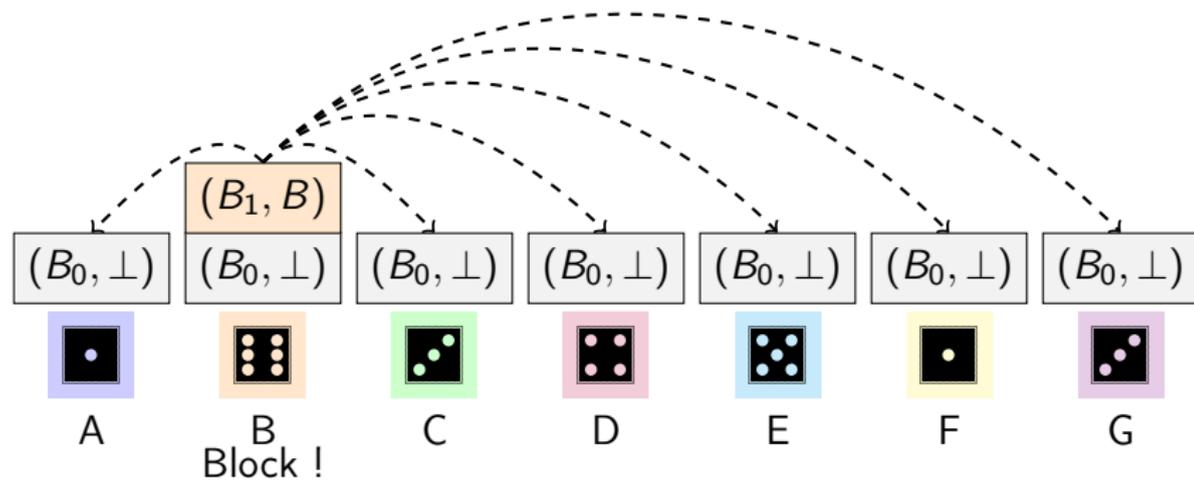
# Blockchain construction



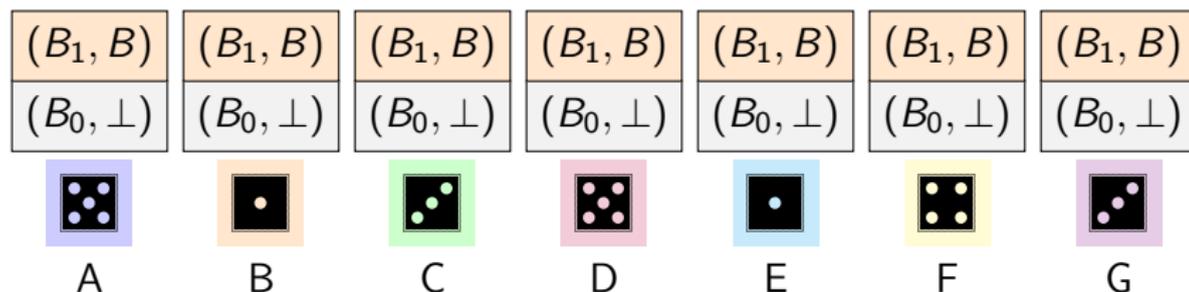
# Blockchain construction



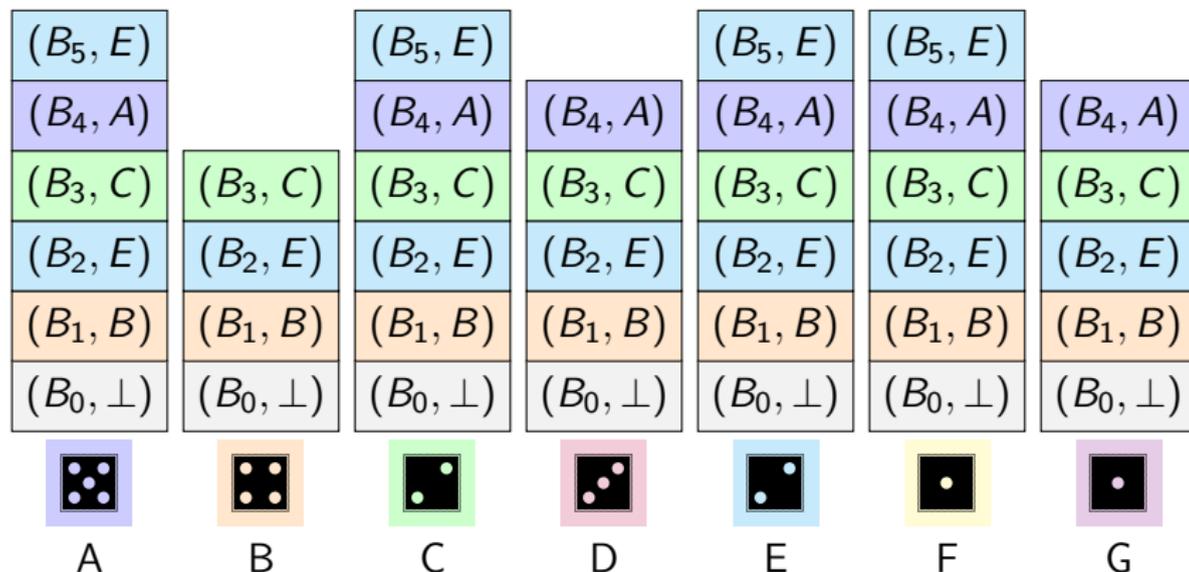
# Blockchain construction



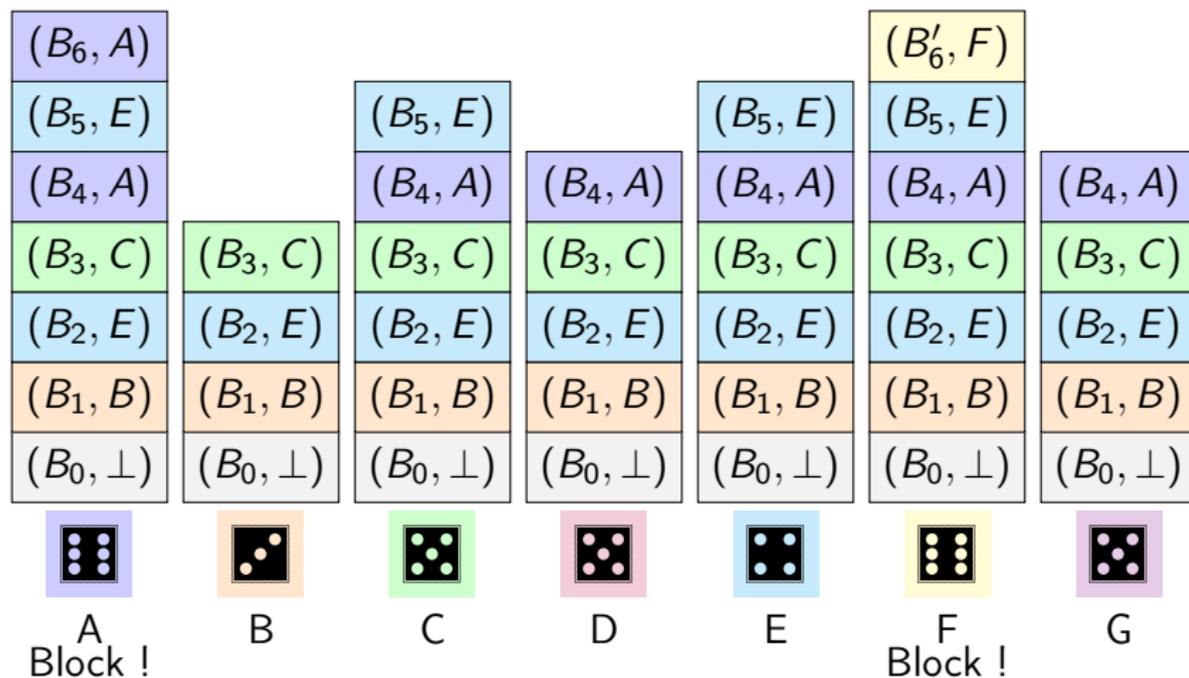
# Blockchain construction



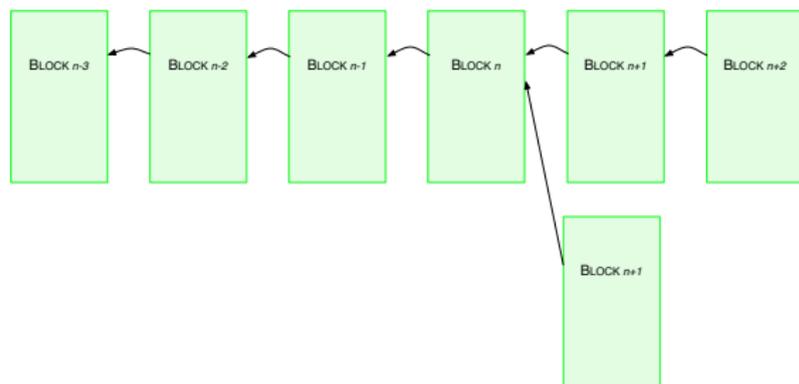
# Blockchain construction



## Conflict : Transient inconsistencies



# Blockchain fork

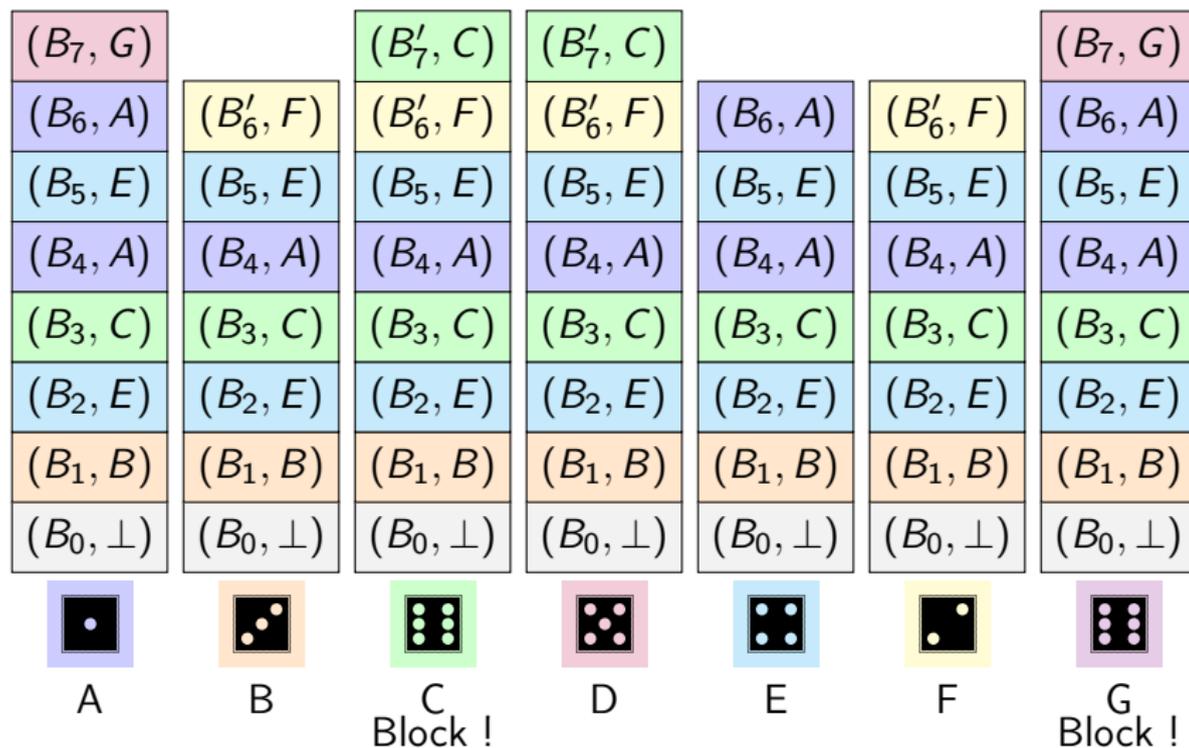


## Nakamoto conflict chain rule

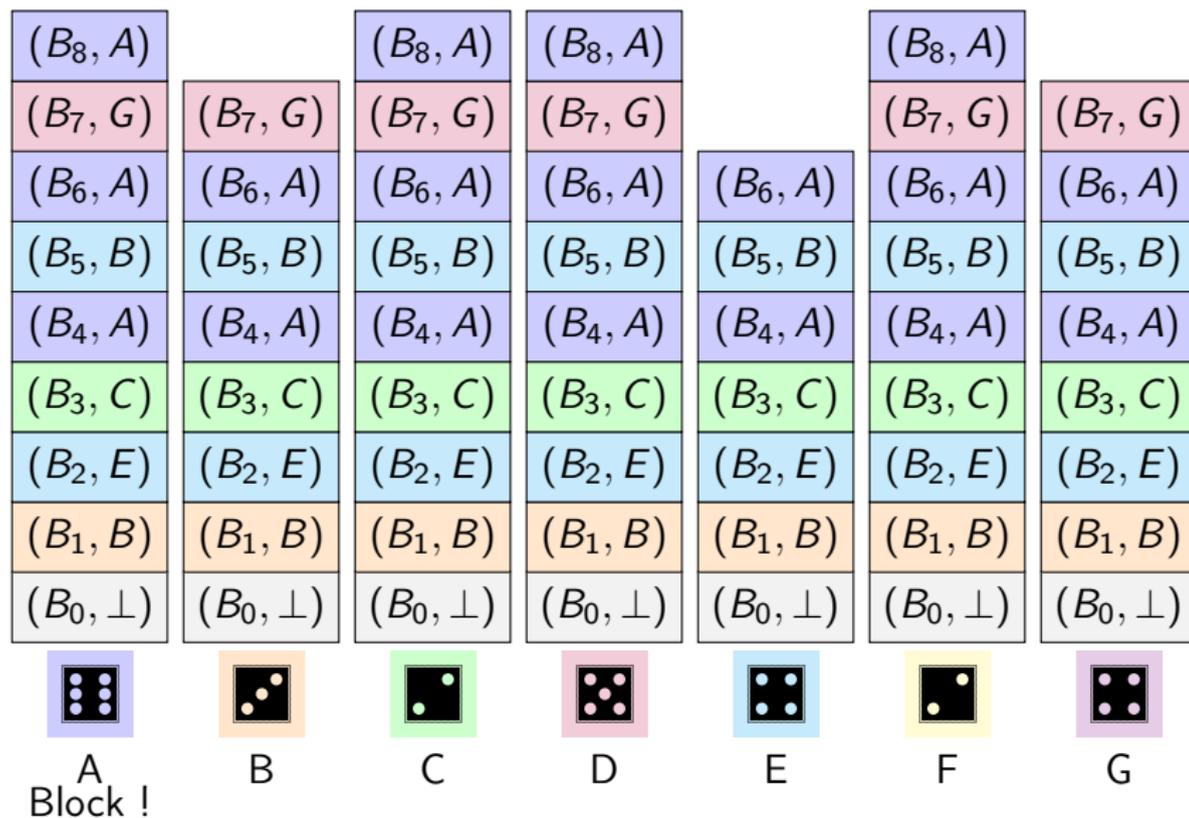
Mine on the longest branch !

- ▶ Proba. that a block is removed from the blockchain decreases exponentially with the number  $k$  of blocks appended to it.
- ▶  $k$  = confirmation level
- ▶ When  $k \geq 6$ , this proba is very small

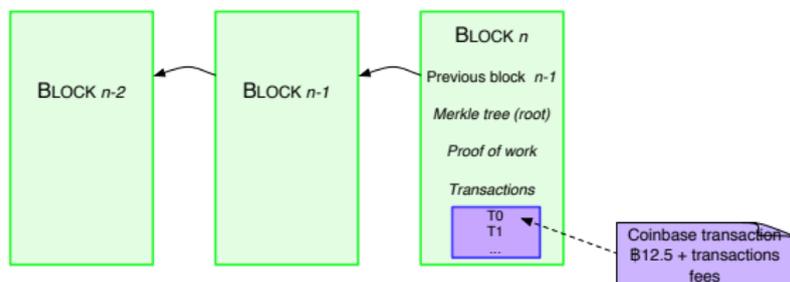
## Conflict : Transient inconsistencies



## Conflict : Transient inconsistencies



## Abstraction 4 : Minting money to incentivize correct behavior



- ▶ Nodes are working (racing) to solve the computational puzzle
- ▶ This is in exchange for monetary rewards
  - ▶ Coinbase transaction = 12.5 bitcoins + transaction fees
  - ▶ Started at 50 bitcoins and is halved every 210,000 blocks
- ▶ This incentivizes miners to only work on valid blocks
  - ▶ « valid block » : for miners, this means blocks for which the majority will accept to build upon

# Summary

- ▶ The bitcoin system relies on a smart combination of abstractions to build a payment system and a crypto-currency
  - ▶ in a completely distributed system (i.e., no trusted third party)
  - ▶ large-scale and open to everyone
  - ▶ incentive to honestly behave (through financial awards)
- ▶ Performance issues : several transactions per second
- ▶ Environmental issues : proof-of-work

# Electing a leader in a permissionless setting

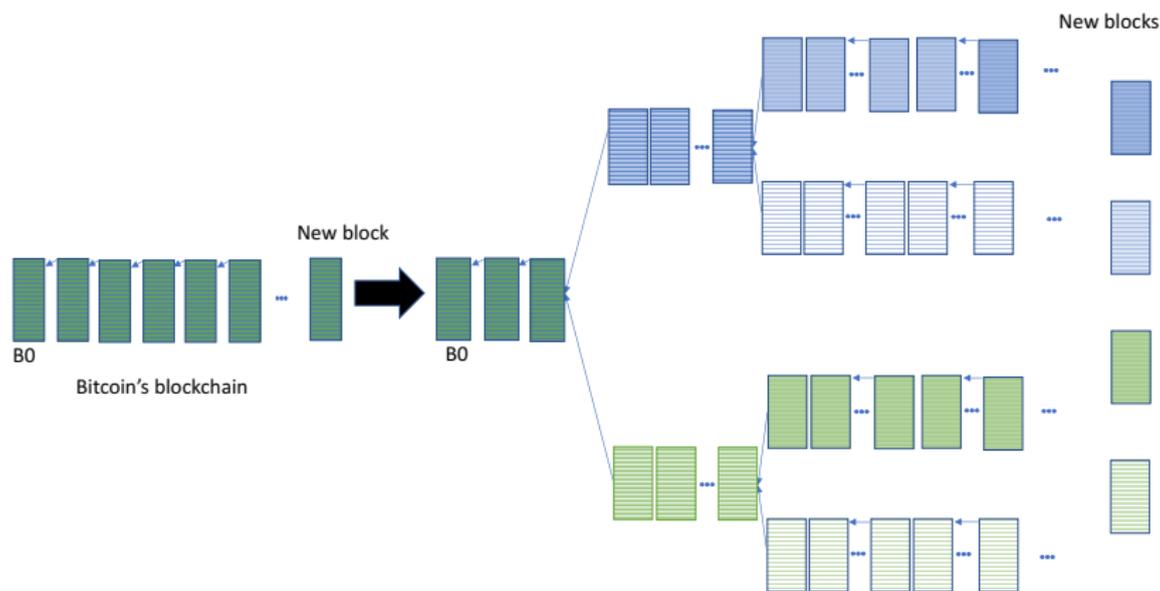
- ▶ Proof-of-work
  - ✓ Works in practice and this is true since 2009
  - ✓ Security analysis
  - ✗ Environmental issues
  - ✗ Diminishing returns
  - ✗ Distinction between miners and crypto-currency holders (i.e., miners control what is inside blocks)
- ▶ Proof-of-work with useful computation, proof-of-space, proof-of-storage, ...
  - ✗ Physical resources
- ▶ Proof-of-stake
  - ✓ Abstract but limited resource : coin itself<sup>8</sup>
  - ✓ All the required information is already in the blockchain
  - ✗ Numerous attacks

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8. A. Durand, E. Anceaume, R. Ludinard, « StakeCube : Combining sharding and proof-of-stake to build fork-free secure permissionless distributed ledgers », Int'l Conference on Networked Systems, 2019

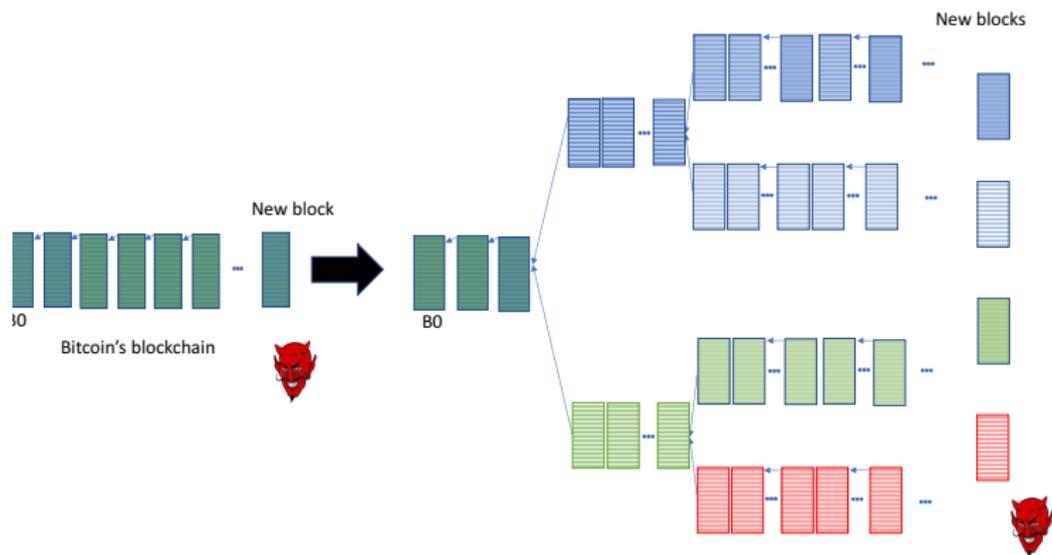
# Self-Adapting to the actual number of transactions

1. A ledger with several parallel (but not conflicting) chains
2. Valid (and not conflicting) blocks should be mined in parallel



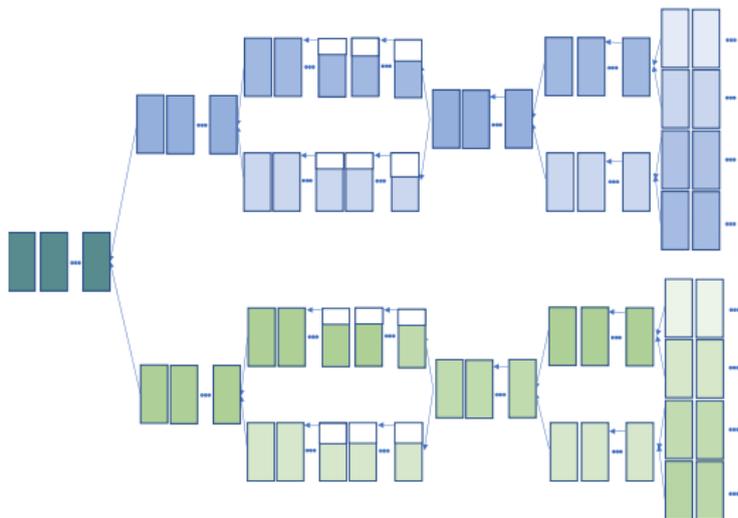
# Self-Adapting to the actual number of transactions

1. A ledger with several parallel (but not conflicting) chains
2. Valid (and not conflicting) blocks should be mined in parallel
3. Miners should not be able to predict the chain of the ledger to which their blocks will be appended
  - ▶ Cannot devote their computational power to a specific chain



## Self-Adapting to the actual number of transactions

1. A ledger with several parallel (but not conflicting) chains
2. Valid (and not conflicting) blocks should be mined in parallel
3. Miners should not be able to predict the chain of the ledger to which their blocks will be appended
4. Overloaded chains should dynamically split and underloaded ones should dynamically merge



⚠ All these features should be verifiable by anyone at any time<sup>9</sup>

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9. E. Anceaume, A. Guellier, R. Ludinard, B. Sericola, Sycomore : a Permissionless Distributed Ledger that self-adapts to Transactions Demand, IEEE NCA, 2018

### Other ways of building distributed ledgers

- ▶ Consortium blockchains
  - ▶ Assume a well-known set of entities capable of the read, write, and execute operations
  - ▶ Do not necessarily require to solve a challenge to write a new block
  - ▶ Rely on Byzantine agreement algorithms
- ▶ Private blockchains
  - ▶ Assume the presence of a trusted third party in charge of the read, write, and execute operations<sup>10</sup>
  - ▶ Do not need to solve a challenge to write a new block
  - ▶ Do not need Byzantine agreement algorithms

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10. Haber and Stornetta, How to timestamp a digital document, J. of cryptology, 3(2), pp 99–111, 1991

Thank you for your attention  
Any questions?

